



MLR Institute of Technology

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M-I Assignment questions

Unit –I

1. Show that $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & 1 \end{bmatrix}$ satisfies the matrix equation $A^3 - A^2 - 18A - 30I = 0$.
2. Find the rank of $\begin{bmatrix} 1 & 2 & 3 & 0 \\ 2 & 4 & 3 & 2 \\ 3 & 2 & 1 & 3 \\ 4 & 8 & 7 & 5 \end{bmatrix}$
3. For what values of λ & μ do the system of equations
 $x + y + z = 6$
 $x + 2y + 3z = 10$
 $x + 2y + \lambda z = \mu$ have
(a) No solution (b) Unique solution (c) more than one solution
4. Prove that if the equation $x = ay + z$; $y = -2 + ax$; $z = x + y$ are consistent then $a^3 + 3 = 0$
5. Find non-singular matrices P & Q such that PAQ is in the normal form for the matrix $A = \begin{bmatrix} 1 & -1 & -1 \\ 1 & 1 & 1 \\ 5 & 4 & 3 \end{bmatrix}$
6. If $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 0 & -1 & 3 \end{bmatrix}$ Find the non singular matrices P and Q such that PAQ is normal form.
7. Discuss the solution of $x + 2y + 3z = ax$; $3x + y + 2z = ay$; $2x + 3y + z = az$ for all values of a.
8. the system of equations using simple elimination on process
 $x + y + z = 6$ 1. $2x - y + 3z = 4$ $4x + 5y - 10z = 13$
9. Find the inverse in the following
(a) $\begin{bmatrix} 2 & 4 & 3 \\ 0 & 1 & 1 \\ 2 & 2 & -1 \end{bmatrix}$ (b) $\begin{bmatrix} 1 & 6 & 4 \\ 0 & 2 & 3 \\ 0 & 1 & 2 \end{bmatrix}$
10. Find the inverse of the matrix
 $A = \begin{bmatrix} 1 & -1 & 1 \\ 1 & -2 & 4 \\ 1 & 2 & 2 \end{bmatrix}$ Using Gauss elimination method.
11. Reduce the following matrix to the tridiagonal form by House holder's method.
a) $\begin{bmatrix} 1 & 3 & 4 \\ 3 & 1 & 2 \\ 4 & 2 & 1 \end{bmatrix}$
12. Solve the system of equations

$$83x + 11y - 4z = 95 \quad 7x + 52y + 13z = 104$$

13. Find Eigen values and Eigen vectors of $A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$
14. Verify Cayley – Hamilton theorem for $A = \begin{bmatrix} 2 & -1 & 1 \\ 1 & 1 & -1 \\ -1 & -2 & 2 \end{bmatrix}$
15. Diagonalise the matrix $A = \begin{bmatrix} -1 & 1 & 2 \\ 0 & -2 & 1 \\ 0 & 0 & -3 \end{bmatrix}$
16. Using Cayley – Hamilton theorem find the inverse of $\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$
17. If $A = \begin{bmatrix} 2+i & 3 & -1+3i \\ -5 & i & 4-2i \end{bmatrix}$ verify that A^*A is a Hermitian matrix
18. Reduce $3x^2 + 3z^2 + 4xy + 8xz + 8yz$ into canonical form.
19. Reduce $3x^2 - 3y^2 - z^2 - 4xy + 8xz + 12yz$ into canonical form by orthogonal transformations and also find its rank, index and signature.
20. Find the Eigen values of $A = 11 \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$ and hence reduce $2xy + 2yz + 2zx$ into canonical form.
21. Using Cayley – Hamilton theorem find the inverse of $\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$
22. Prove that $A = \frac{1}{2} \begin{bmatrix} 1+i & -1+i \\ 1+i & 1-i \end{bmatrix}$ is unitary.
23. Prove that eigen values of Hermitian matrix are real.

Unit –II

- Verify the Rolle's Theorem for the function $f(x) = (x-a)^m (x-b)^n$ in $[a, b]$.
- Verify the Rolle's Theorem for following the function.
 - $f(x) = e^x (\sin x - \cos x)$ in $[\pi/4, 5\pi/4]$
 - $f(x) = x(x+3)e^{-x/2}$ in $[-3, 0]$
- Using mean value theorems show that $\pi/4 + 3/25 < \tan^{-1} 4/3 < \pi/4 + 1/6$
- Find Maclaurin's theorem with Lagrange's form of remainder for $f(x) = \cos x$.
- A rectangular box open at the top is to have volume of 32 cubic ft. Find the dimensions of the box requiring least material of its construction.
- Expand $x^2y + 3y - 2$ in powers of $x-y$ and $y+2$ upto the terms of 3rd degree. Using Taylor's theorem.
- Find the minimum value of $x^2 + y^2 + z^2$ when $ax + by + cz = p$.

Unit –III

- Evaluate $\iiint xyz \, dx dy dz$ over the positive octant of the sphere $x^2 + y^2 + z^2 = a^2$
- Show that $\int_a^b (x-a)^m (b-x)^n dx = (b-a)^{m+n+1} \beta(m+1, n+1)$
- Show that $\int_0^\infty x^4 e^{-x^2} dx = \frac{3\sqrt{\pi}}{8}$

4. Show that $\beta(m,n) = \int_0^{\infty} \frac{y^{n-1}}{(1+y)^{m+n}} dy$

5. Evaluate $\int_0^1 x^3 \sqrt{1-x} dx$ using $\beta - \Gamma$ functions.

Unit -IV

1. Find the equation of the curve passing through the point (0, -1) and whose differential equation is

$$(1 + y^2)dx + (1 + x^2)dy = 0.$$

2. Eliminate the arbitrary constants and obtain the DE for following.

a. $x^2 + y^2 + 2gx + 2fy + c = 0$ b. $\tan x \tan y = c$ (c). $x \tan(y/x) = c$ (c).

3. Solve $(x^2 + y^2)dx = 2xy dy$.

4. Solve $x dy/dx + y = \log x$.

5. Solve $dr + (2r \cot\theta + \sin 2\theta)d\theta = 0$.

6. Solve $x dy/dx + y = x^3 y^6$.

7. Solve $(1 - x^2) dy/dx + xy = y^3 \sin^{-1} x$.

8. Find the Orthogonal trajectories of the following family of curves.

a. $x^2/(a^2 + \lambda) + y^2/(b^2 + \lambda) = 1$ b. $r = 2a/(1 + \cos\theta)$.

9. The number N of bacteria in a culture grew at a rate proportional to N. The value of N was initially 100 and increased to 332 in one hour what was the value of N after 1½ hours

10. A body is originally at 80°C and cools down to 60°C in 20 minutes. If the temperature of the air is 40°C, find the temperature of the body after 40 minutes

11. Solve $y^{11} + y^1 - 2y = 0$ $y(0) = 4$, $y^1(0) = 1$.

12. Solve $(D^3 + 1)y = 3 + 5e^x$.

13. Solve $y^{11} + 4y^1 + 4y = 4\cos x + 3\sin x$, $y(0) = 3$.

14. Solve $(x^3 D^3 + 2x^2 D^2 + 2)y = 10(x + 1/x)$

15. $(D^2 + 3D + 2)y = e^{2x} + x^2$.

16. Solve $(D^3 + 2D^2 + D)y = e^{2x} + x^2 + x + \sin 2x$.

17. using variation of parameters solve $(D^2 + 1)y = \operatorname{cosec} 2x$

Unit -V

1. Find the Laplace transform of the following

a. $\frac{1-\cos t}{t}$ b. $e^{-3t}\cos 4t$ c. $e^{2t}+4t^3-2\sin 3t+3\cos 3t$ d. $\sin (wt+\alpha)$, α is a constant

2. $(e^{-at}-e^{-bt})/t$

3. $\int_0^t e^t \frac{\sin t}{t} dt$

4. Find the inverse Laplace transform of the following functions

i. $\frac{3(s-1)^2}{2s^5}$ ii. $\frac{s^2}{s^4-a^4}$ iii. $\frac{4}{(s-1)(s+2)}$ iv. $\frac{1}{s^2+25} \sin (wt+\alpha)$, α is a constant

v. $\text{Log} \frac{s+1}{s-1}$ vi. $\text{Cot}^{-1}s$

5. $\frac{s}{(s^2+a^2)(s^2+b^2)}$ by convolution theorem

6. Solve the following boundary value problems by using Laplace transforms

i. Solve $(D^2+1)x=t\cos 2t$ given $x=0$, $x'(t)=0$ at $t=0$. ii. $y^{(11)}+2y^{(11)}-y'-2y=0$ with $y(0)=y'(0)=0$ and $y^{(11)}(0)=6$